

BAREM DE CORECTARE

PARTEA ÎNTÂI

1.	2.	3.	4.	5.	6.	7.	8.	9.
D. 6	D.24	D.1	C. $\{-1\} \cup$ $[\frac{1}{3}, +\infty)$	C.3	A.160	B. $\frac{(a^2+b^2)^2}{b^2}$	A.160	A. $80\sqrt{30}$

PARTEA A DOUA

1a.	a) $[-7,25] + \{-7,25\} = -8 + 0,75 = -7,25$	6p
b.	$\left[\frac{3x-2}{7}\right] = x - 6 \Rightarrow x - 6 \leq \frac{3x-2}{7} < x - 5 \Rightarrow$ $7x - 42 \leq 3x - 2 < 7x - 35 \Rightarrow$ $x \in \{9,10\}$	2p 2p 2p
c.	$36^{[x]} + 6^{[x]+\{x\}} = 7 \cdot 6^{[x]} / 6^{[x]} \neq 0 \Rightarrow$ $6^{[x]} + 6^{\{x\}} = 7.$ Discuție Pentru $x < 0 \Rightarrow 6^{[x]} < 1$ $6^{\{x\}} < 6$ nu convine Pentru $x > 1$ $6^{[x]} + 6^{\{x\}} > 7$ nu convine Pentru $x \in (0,1)$ $6^{[x]} = 1$, $6^{\{x\}} < 6$ nu convine Pentru $x = 1$ avem $6 + 1 = 7.$ Pentru $x=0$ avem $1+1=2$ nu convine	2p 2p 2p
2a.	a) $BC^2 + AB^2 + A'A^2 = 289$ $AB^2 + BC^2 + A'A^2 - 2(8BC + 12AB + 9AA') = -289$ $BC^2 - 2 \cdot 8 \cdot BC + 64 + AB^2 - 2 \cdot 12AB + 144 + AA'^2 - 2 \cdot 9AA' + 81 = 0$ $(BC-8)^2 + (AB-12)^2 + (AA'-9)^2 = 0 \Rightarrow BC = 8\text{cm}; AB = 12\text{cm}; AA' = 9\text{cm}$ Suma ariilor fețelor laterale = $2AB \cdot AA' + 2BC \cdot AA' = 2 \cdot 9 \cdot 20 = 360 \text{ cm}^2$	1p 2p 2p 1p
b.	a) $AM = 2MB \Rightarrow MB = 12 : 3 = 4 \text{ cm}$ $BC = 2BN \Rightarrow BN = 8 : 2 = 4 \text{ cm}$ $\Rightarrow \Delta MBN = \text{dreptunghic isoscel} \Rightarrow \sphericalangle MNB = 45^\circ$ $A'D' \parallel BC \Rightarrow (\widehat{A'D'}, \widehat{MN}) = (\widehat{BC}, \widehat{MN}) = 45^\circ$	3p 3p
c.	a) $D'C = \sqrt{12^2 + 9^2} = \sqrt{225} = 15 \text{ cm}$ $CN = 4 \text{ cm}$ $D'N = \sqrt{15^2 + 16} = \sqrt{241} \Rightarrow D'N^2 = 241$ $D'M = \sqrt{8^2 + 9^2 + 8^2} = \sqrt{209} \Rightarrow D'M^2 = 209$ $MN^2 = 32$ $\sphericalangle M = 90^\circ \Rightarrow \sin(\widehat{MD'N}) = \frac{MN}{D'N} = \frac{4\sqrt{2}}{\sqrt{241}}$	2p 2p 2p